CALCULUS II
GRADE LEVEL 12

| \# | Lesson | Lesson Content |
| :---: | :---: | :---: |
| 1 | Definite Integrals | Definition of integral, discussion of finding integrals, notations for integrals, discussion of definite integrals |
| 2 | Fundamental Theorem | Implications of the fundamental theorem of calculus, evaluating definite integrals, addition property |
| 3 | Indefinite Integrals | The integral as a function; antiderivatives, integrating a constant multiple of a function |
| 4 | Integrals by Substitution | Inverse of the chain rule, determining $u$ and du, integrals of the squares of sine and cosine; substitution for definite integrals/change limits |
| 5 | Natural Logarithms | Definition of natural logarithm as an integral; review of laws of logarithms; derivatives of natural logarithms; finding the integral of tangent using logarithms |
| 6 | Area Between Two Graphs | Discussion of implications of areas between graphs; points of intersection for region; comparing functions for subtraction direction |
| 7 | Integral Unit Review | Review of integrals, antiderivatives, chain rule, logarithms, laws of logarithms, and other material covered in previous lessons |
| 8 | Volumes 1 | Volumes of rotation of $\mathrm{F}(\mathrm{x})$ about the x -axis; the disc method; the washer method (two functions) |
| 9 | Volumes 2 | Volumes of rotation $\mathrm{F}(\mathrm{x})$ about the y -axis; the shell method, the shell method with two functions |
| 10 | Arclength | Definition and examples of arclength, finding the length of a curve |
| 11 | Surface Area | Finding the area of a rotational surface |
| 12 | Work | Definition of work; finding work with a variable force; work to empty a tank |
| 13 | Application Unit Review | Review of volumes, surface area, work, and hydrostatic force |
| 14 | Exponent Function | The natural exponent function; inverse of the natural logarithm; laws of exponents; derivative of the natural exponent; integral of the natural exponent |
| 15 | Exponents and Logarithms | Exponential and logarithmic functions of other bases; rewriting exponentials with the natural exponential; derivative of general exponential functions; logarithms of different bases; derivative of general logarithms |
| 16 | Growth and Decay | Exponential growth and decay; function of exponential growth and decay; half-lives and doubling times |
| 17 | Inverse Trig Functions | Arcsine and arccosine; arctangent and arccotangent; arcsecant and arccosecant; derivatives and integrals of all six functions |
| 18 | Inverse Functions Review | Review of exponents, logarithms, and inverse trig functions |
| 19 | Integration by Parts | Breaking up the function to be integrated; nth powers of sine and cosine |
| 20 | Trigonometric Integrals | Integrals involving trigonometric functions; products of sines and cosines; products of tangents and secants; changing to sines and cosines; using trig identities |
| 21 | Trig Substitutions | Substitution trig functions in for x ' forms containing square roots and x squared |
| 22 | Partial Fractions | Preparing the fraction; division; factoring; breaking the fraction into its component parts |
| 23 | Approximations | Using trapezoidal rule to approximate area; using Simpson's rule to |


|  |  | approximate area |
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| 24 | Improper Integrals | Unbounded integrands; unbounded intervals; convergent or divergent <br> integrals |
| 25 | Techniques Unit Review | Review of previous material |
| 26 | Comprehensive Exam |  |

